

# MODEL FOR ION-ASSISTED FILM GROWTH

A.S. Bakai, S.N. Sleptsov, A.I. Zhukov  
NSC "KhFTI

A new model of growing film densification is proposed. The model takes into account the diffusional mobility of point defects and interaction between them. The film density as a function of ion flux, ion energy and substrate temperature is investigated.

## 1. Introduction

Vapor-deposited thin films have a lower density than the corresponding bulk material. This is caused by a low mobility of surface atoms thus vacancies and their complexes are formed [1]. It is possible to increase the density of vapor-deposited films by self or gas ions bombardment during growth [2]. Muller has proposed a model for ion-assisted film densification [3]. This model explains the experimentally observed increase in the film density for the low ion fluxes case, but it leads to unreasonable results for large ion fluxes: the film density exceeds the one of the bulk material. This discrepancy is mainly due to by neglecting of point defects mobility.

We present a model, where the diffusion of point defects is taken into account. Satisfactory description of experimental data is obtained in the frame of our model.

## 2. Diffusion model of densification

Let us denote the fluxes of condensing atoms and gas ions as  $J_n$  and  $J_g$  respectively and the film growth rate as  $V$ . Ions penetrate into the film and produce interstitials and vacancies. In moving coordinate system, connected with surface ( $x = 0$ ), the concentrations of interstitials  $C_i$ , vacancies  $C_v$ , implanted gas atoms  $C_g$  and gas-vacancy complexes  $C_c$  can be described by the following diffusion equations:

$$\frac{d}{dx} \left( D_i \frac{d}{dx} C_i \right) - V \frac{d}{dx} C_i - \alpha_{iv} C_i C_v - \alpha_{ic} C_i C_c + Q_i(x) = 0, \quad (1)$$

$$\frac{d}{dx} \left( D_v \frac{d}{dx} C_v \right) - V \frac{d}{dx} C_v - \alpha_{iv} C_v C_i - \alpha_{gv} C_v C_g + \omega_c C_c + Q_v(x) = 0, \quad (2)$$

$$\frac{d}{dx} \left( D_g \frac{d}{dx} C_g \right) - V \frac{d}{dx} C_g - \alpha_{gv} C_g C_v + \alpha_{ic} C_i C_c + \omega_c C_c + Q_g(x) = 0, \quad (3)$$

$$\frac{d}{dx} \left( D_c \frac{d}{dx} C_c \right) - V \frac{d}{dx} C_c - \alpha_{ic} C_c C_i + \alpha_{gv} C_g C_v - \omega_c C_c = 0. \quad (4)$$

Here,  $D_{i,v,g,c}$  are the diffusion coefficients of interstitials, vacancies, gas atoms and complexes respectively,  $D_\alpha = D_{0\alpha} \exp(-E_\alpha^m / kT)$ ,  $E_\alpha^m$  are the migration energies,  $\alpha = i, v, g, c$ ;  $T$  is the substrate temperature,  $\alpha_{iv,gv,ic}$  and  $\omega_c$  are the constant of reactions in the following processes:

recombination of interstitials and vacancies

$$\alpha_{iv}: i + v = 0,$$

formation of gas + vacancy complexes

$$\alpha_{gv}: g + v = c,$$

recombination of interstitials and vacancies in gas-vacancy complexes

$$\alpha_{iv}: i + c = i + v + g = g,$$

thermal decaying of gas-vacancy complexes

$$\omega_c \cdot c = g + v.$$

All of constants a have the following form

$$\alpha_{ab} = \frac{4\pi R_{ab}}{\Omega} (D_a + D_b), \quad (5)$$

where  $R_{ab}$ , are the reactions' radii,  $\Omega$  is the atom volume, and

$$\omega_c = \omega_d \exp(-E_c^d / kT), \quad (6)$$

where  $\omega_d$  is the vibration frequency factor for gas-vacancy complex,  $E_c^d$  is the dissociation energy of gas-vacancy complex. In Eqs. (1)-(4)  $Q_{j, v, g}(x)$  are the generation rates of interstitials, vacancies and implanted gas atoms respectively.

Without irradiation, i.e. at  $Q_{j, v, g} \equiv 0$ , Eqs.(1)-(4) have to describe the film growth with atom density  $\rho_0 < 1$ . Therefore we choose assume the next boundary condition for vacancies

$$C_v(0) = C_v^0, \quad (7)$$

where  $C_v^0 = 1 - \rho_0$ . The boundary concentration  $C_v^0$  depends on vapor flux and temperature.

Suppose that the surface is ideal sink for interstitials, implanted gas atoms and gas-vacancy complexes:

$$C_{i, g, c}(0) = 0. \quad (8)$$

At far distance from surface, i.e. with  $x \rightarrow \infty$  the point defects fluxes are absent:

$$\frac{d}{dx} C_{i, v, g, c}(\infty) = 0 \quad (9)$$

Eqs. (1)-(4) should be complemented by an equation for determination of the surface velocity  $V$ .  $J_n \Delta t \Delta S$  atoms fall on surface square  $\Delta S$  during time  $\Delta t$  and  $J_g Y \Delta t \Delta S$  atoms ( $Y$  is the sputtering coefficient) leave the surface. The total number of atoms in the film increase:

$\Delta N = (J_n - J_g Y) \Delta t \Delta S$ . From the other hand,  $\Delta N$  can be written as  $V \Delta t \Delta S \rho(\infty) \Omega^{-1}$ , therefore

$$V = \frac{J_n - J_g Y}{1 - C_i(\infty) - C_c(\infty) + C_i(\infty)} \Omega. \quad (10)$$

Follow Ref.[3], let us describe the densification by the next way. The vacancies which are created in thin layer  $d$  refilled by arriving vapor atom or interstitials, so we change generation rates of vacancies and interstitials in this layer as

$$Q_v^{eff}(0 \leq x \leq \delta) = 0, \quad Q_i^{eff}(0 \leq x \leq \delta) = \max[0, Q_i(x) - Q_v(x)]. \quad (11)$$

From Eqs. (1)-(4), (10) with boundary conditions (7)-(9) one can find the film density  $\rho_f$ , i.e. density with  $x \rightarrow \infty$ :

$$\rho_f \equiv \rho(\infty) = 1 - C_v(\infty) - C_c(\infty) + C_i(\infty). \quad (12)$$

### 3. Calculations

Let us consider the growth of vapor-deposited Cr films which is bombarded with low-energy  $Ar^+$  ions. The parameters of irradiation and material constants, which are used in Eqs.(1)-(4), (10) are shown in Table. The profiles of generated point defects, implanted gas atoms and the sputtering coefficients are calculated by the code SPURT [4], which is similar to the cascade code TRIM [5]. Nonlinear Eqs.(1)-(4), (10) are solved by finite element method.

Figure 1 shows the film density versus ion flux at different temperatures. The curve obtained at  $T=0$  K corresponds to the Muller's model [3]. One can see that taking into account the

diffusional mobility of interstitials limits the growth of film density and it does not exceed the density of bulk material.

Figure 2 shows the film density versus ion energy at different ratios ion-to-vapor fluxes.

#### 4. Conclusion

The proposed model of ion-assisted growth of vapor-deposited films correctly describes the film densification at high ion fluxes at the temperature, when interstitials are mobile.

#### REFERENCES

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Table. Material parameters used for calculation.

Interstitial diffusivity pre-exponential	$0.015 \text{ cm}^2 \text{ s}^{-1}$	Interstitial migration energy	0.15 eV
Vacancy diffusivity pre-exponential	$0.300 \text{ cm}^2 \text{ s}^{-1}$	Vacancy migration energy	1.10 eV
Argon diffusivity pre-exponential	$0.075 \text{ cm}^2 \text{ s}^{-1}$	Argon migration energy	0.30 eV
Gas-vacancy diffusivity preexponential	$10^{\wedge} \text{ cm}^2 \text{ s}^{-1}$	Migration energy of gas-vacancy complex	4.50 eV
Vibration frequency factor for gas-vacancy complex	$1.3 \times 10^{13} \text{ s}^{-1}$	Dissociation energy of gas-vacancy complex	1.30 eV
Recombination radius, $R_{iv}$	0.580 nm	Trapping radius, $R_{gv} \sim R_{ic}$	0,75 nm
Atom volume	$12 \times 10^{-24} \text{ cm}^3$	Vapor flux	$3.75 \times 10^{16} \text{ cm}^{-2} \text{ s}^{-1}$
Depth of $\delta$ -layer	0.410 nm	Constant lattice	0.29 nm

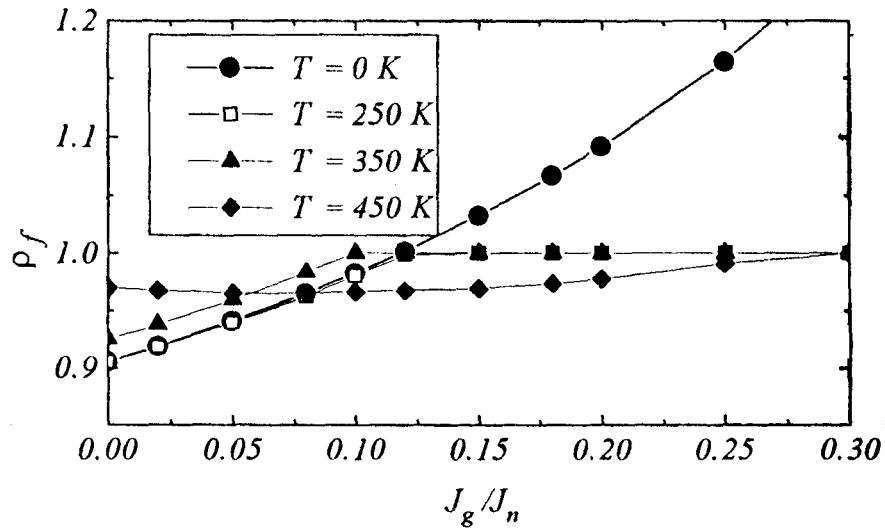


Fig. 1. Relative density as a function of ratios of ion-to vapor fluxes

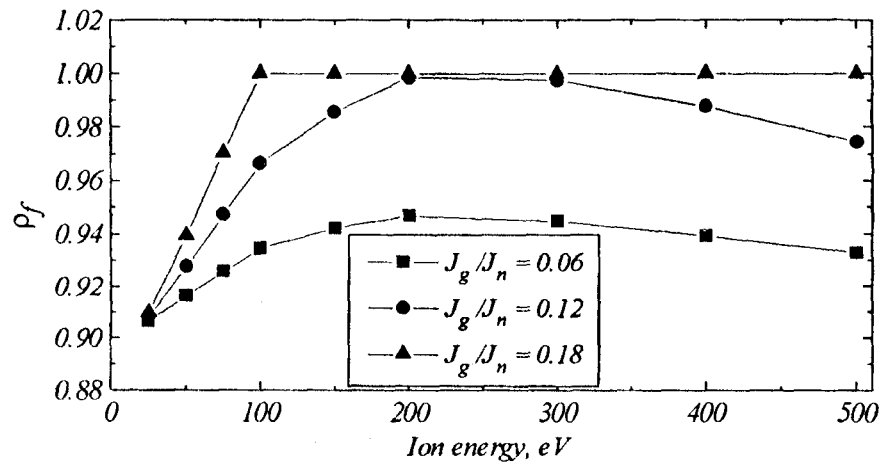


Fig. 2. Relative density as a function of ion energy at  $T = 300\text{ K}$